

P 72-73

WALKING

A. Weighted Voting Systems

1. Consider the weighted voting system $[13: 7, 4, 3, 3, 2, 1]$. Find
 - (a) the total number of players
 - (b) the total number of votes
 - (c) the weight of P_2
 - (d) the minimum percentage of the votes needed to pass a motion (rounded to the next whole percent)

3. Consider the weighted voting system $[q: 10, 6, 5, 4, 2]$.
 - (a) What is the smallest value that the quota q can take?
 - (b) What is the largest value that the quota q can take?
 - (c) What is the value of the quota if *at least* two-thirds of the votes are required to pass a motion?
 - (d) What is the value of the quota if *more* than two-thirds of the votes are required to pass a motion?

5. A committee has four members ($P_1, P_2, P_3,$ and P_4). In this committee P_1 has twice as many votes as P_2 ; P_2 has twice as many votes as P_3 ; P_3 has twice as many votes as P_4 . Describe the committee as a weighted voting system when the requirements to pass a motion are
 - (a) at least two-thirds of the votes
 - (b) more than two-thirds of the votes
 - (c) at least 80% of the votes
 - (d) more than 80% of the votes

7. In each of the following weighted voting systems, determine which players, if any, (i) are dictators; (ii) have veto power; (iii) are dummies.
 - (a) $[6: 4, 2, 1]$
 - (b) $[6: 7, 3, 1]$
 - (c) $[6: 5, 5, 1]$

9. In each of the following weighted voting systems, determine which players, if any, (i) are dictators; (ii) have veto power; (iii) are dummies.
 - (a) $[19: 9, 7, 5, 3, 1]$
 - (b) $[15: 16, 8, 4, 1]$
 - (c) $[17: 13, 5, 2, 1]$
 - (d) $[25: 12, 8, 4, 2]$